# Maximizing Network Throughput in Heterogeneous UAV Networks

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Abstract-In this paper we study the deployment of an Unmanned Aerial Vehicle (UAV) network that consists of multiple UAVs to provide emergent communication service for people who are trapped in a disaster area, where each UAV is equipped with a base station that has limited computing capacity and power supply, and thus can only serve a limited number of people. Unlike most existing studies that focused on homogeneous UAVs, we consider the deployment of heterogeneous UAVs where different UAVs have different computing capacities. We study a problem of deploying K heterogeneous UAVs in the air to form a temporarily connected UAV network such that the network throughput - the number of users served by the UAVs, is maximized, subject to the constraint that the number of people served by each UAV is no greater than its service capacity. We then propose a novel  $O(\sqrt{\frac{s}{K}})$ -approximation algorithm for the problem, where s is a given positive integer with  $1 \le s \le K$ , e.g., s = 3. We also devise an improved heuristic, based on the approximation algorithm. We finally evaluate the performance of the proposed algorithms. Experimental results show that the

Manuscript received 24 May 2023; revised 20 October 2023; accepted 26 November 2023; approved by IEEE/ACM TRANSACTIONS ON NETWORK-ING Editor J. S. Sun. Date of publication 1 January 2024; date of current version 18 June 2024. The work of Wenzheng Xu was supported in part by the National Natural Science Foundation of China (NSFC) under Grant 62272328, in part by the Sichuan Science and Technology Program under Grant 24NSFJQ0152, and in part by the Double World-Class Project for Sichuan University under Grant 0082604151352. The work of Chaocan Xiang was supported by NSFC under Grant 62172063. The work of Jian Peng was supported in part by the Cooperative Program of Sichuan University, Yibin, under Grant 2020CDYB-30; in part by the Cooperative Program of Sichuan University, Zigong, under Grant 2022CDZG-6; in part by the Key Research and Development Program of Sichuan Province, China, under Grant 22ZDYF3599; and in part by the Sichuan Science and Technology Program under Grant 2022ZDZX0011. (Shuyue Li and Chaocan Xiang are co-first authors.) (Corresponding author: Wenzheng Xu.)

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This article has supplementary downloadable material available at https://doi.org/10.1109/TNET.2023.3347557, provided by the authors.

Digital Object Identifier 10.1109/TNET.2023.3347557

numbers of users served by UAVs in the solutions delivered by the proposed algorithms are increased by 25% than state-of-the-arts.

Index Terms—UAV communication networks, UAV deployment problem, heterogeneous UAVs, approximation algorithms.

#### I. Introduction

TERRESTRIAL LTE base stations usually are statically deployed. However, this static deployment limits their usage in key 5G and 5G Beyond applications with surging traffic demands at some hotspot locations (e.g., battlefields and concerts). In addition, the deployed base stations may have been destroyed in natural disasters, e.g., earthquakes, tsunamis, flooding, etc. Emergent communication service are definitely needed for rescue teams to rescue people trapped in disaster areas [9], [19].

The employment of Unmanned Aerial Vehicles (UAVs) or drones, e.g., DJI Matrice 300 RTK UAVs, has gained great attention in public safety communications [5], [9], [20], [22], [25], [27], [35], [37], [38], [45]. By installing an LTE base station on a UAV, the UAV can provide wireless communication service to ground users in the air [3], [26]. The LTE base station usually consists of two modules: SkyRAN and SkyCore, where SkyRAN provides wireless connectivity to ground users, while SkyCore is responsible for user mobility, management, control functions, and routing [26], [34]. In addition, some mobile operators, e.g., AT&T and Verizon, conducted experiments about UAVs with mounted LTE base stations [26]. A UAV communication network that consists of multiple UAVs can be easily deployed to provide emergent communication service in a disaster area, see Fig. 1. Both rescue teams and the people trapped can communicate with each other by leveraging the deployed UAV network.

In spite of the aforementioned promising applications of UAV networks, there are many challenges to realize these applications. Particularly, since the payload of each UAV usually is very limited, e.g., the maximum payload of a DJI Matrice 300 RTK UAV is only 2.7 kg [7], many functions in the SkyCore module must run in a low-end, light-weight server with a very resource-constrained CPU and a small-capacity battery, where the server is mounted on the UAV [3]. This could significantly increase the processing (control and data plane) latency of its traffic, thereby reducing network throughput [26]. Thus, a UAV usually needs to restrict the number of users it can serve, i.e., there is a *service capacity* 

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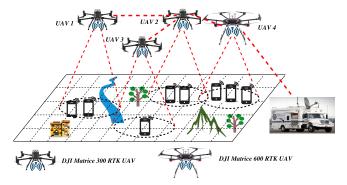


Fig. 1. A heterogeneous UAV network can provide communication service to people who are trapped in a disaster area, where UAVs 1, 2, and 3 are DJI Matrice 300 RTK, while UAV 4 is DJI Matrice 600 RTK and it is connected to the Internet through the relay of an emergency communication vehicle

on each UAV [40], [46], e.g., 200 users. Otherwise, if a UAV serves too many users, each of the users may experience a very long service delay, e.g., a few seconds, and the network throughput also significantly decreases [26].

#### A. Motivation

The deployment of resource-constrained UAV networks recently has attracted a lot of attentions [10], [21], [30], [32], [39], [40], [41], [42], [46]. Most existing studies assumed that the UAVs are *homogeneous*. Different from these existing studies, in this paper we consider the deployment of *hetero*geneous UAVs. There are two major reasons for employing heterogenous UAVs. The first reason is that the UAVs owned by a rescue team usually are used for multiple disasters (e.g., earthquakes, flooding, tsunamis, etc.), not only for a single disaster. Therefore, the rescue team needs to purchase different types of UAVs for the usages in different disaster scenarios. The second reason is that the UAVs owned by the rescue team may be purchased at different time periods. Some UAVs bought a few years ago may not be available in the current market, while recently purchased UAVs, even made by the same company, have different payloads and battery capacities. For example, consider two popular UAVs for emergency communications: DJI Matrice 600 RTK UAV and DJI Matrice 300 RTK UAV. The former has a maximum payload of 5.5 kg [6] but it is out of production line now, while the latter has a maximum payload of 2.7 kg only and is available in the market [7]. In addition, heterogeneous UAVs are widely used in real post-disaster emergency communications. For example, in the Luding earthquake of China in 2022, pterosaur-2H UAVs and double-tailed scorpion TB UAVs were used in the disaster area to provide communication service [8], [29].

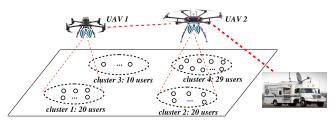
Due to different maximum payloads and energy capacities on different UAVs, the base stations mounted on different UAVs may be different too. The base station on a DJI Matrice 600 RTK UAV may be more powerful than the one on a DJI Matrice 300 RTK UAV, in terms of computing capability and/or battery capacity, thus the former is able to serve more users, i.e., has a larger *service capacity*. Fig. 1 illustrates such a heterogeneous UAV network.

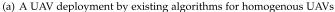
#### B. Novelty

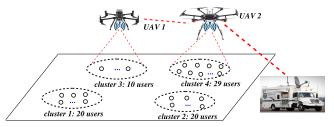
In this paper, we consider the deployment of a UAV network that consists of multiple heterogeneous UAVs in a disaster area, so as to provide emergent communication service to ground users who are trapped in the area. We study a novel maximum connected coverage problem, which is to deploy K heterogeneous UAVs to serve users such that the number of users served by the deployed UAVs is maximized, subject to that (i) the number of users served by each UAV is no greater than its service capacity; (ii) the data rate of each user served by a UAV is no less than his/her minimum data rate requirement; and (iii) the UAV communication network must be connected as the data from the users served by one UAV must be sent to the users served by another UAV, e.g., the communications between trapped people and rescue teams.

A potential solution to the maximum connected coverage problem is that, the to-be-deployed K UAVs are assumed to be homogeneous and their uniform service capacity is assumed as the average service capacity of the original heterogeneous UAVs, K hovering locations of the UAVs then are identified, by applying one of existing algorithms in [10], [21], [30], [40], [42], and [46]. Finally, the K original UAVs with different service capacities are deployed at the K chosen hovering locations in a greedy way. That is, assume that the service capacities of the K UAVs are sorted in non-increasing order. The kth UAV is deployed at one of the K locations with the maximum new increased number of served users, while ensuring that the location was not deployed by any UAV previously, where  $1 \le k \le K$ . For example, assume that K(=2) UAVs need to be deployed to serve four clusters of users, where there are 20, 20, 10, 29 users in the four clusters, respectively, and the service capacities of the two UAVs are 10 and 30 users, respectively, see Fig. 2(a). The average service capacity of the two UAVs is  $20 \ (= \frac{10+30}{2})$  users. Existing algorithms for the homogeneous UAV deployment may identify two hovering locations above clusters 1 and 2, since 40 users will be served if the UAVs were homogeneous, see Fig. 2(a). The two original heterogeneous UAVs are deployed at the two hovering locations, respectively. It can be seen that only 30 (= 10 + 20) users will be served by the two deployed UAVs, since the service capacity on UAV 1 is 10 users only. In contrast, Fig. 2(b) shows that 39(=10+29) users will be served in the optimal deployment with heterogeneous UAVs. It can be seen from the example in Fig. 2 that, less users will be served if we apply the exiting algorithms for the homogeneous UAV deployment to the scenario with heterogeneous UAVs. New algorithms for the heterogeneous UAV deployment are desperately needed.

The heterogeneous UAV deployment problem is very challenging, since the objective of the problem, i.e., serving more users, conflicts with the network connectivity constraint, which is explained as follows. On one hand, to serve as many users as possible, the UAVs should be deployed over locations with high-density users. However, such locations may be far away from each other. The resulting UAV network may not be connected. On the other hand, to ensure the connectivity of deployed UAVs, the UAVs should not be deployed too far







(b) the optimal deployment with heterogeneous UAVs

Fig. 2. A comparison between a UAV deployment by existing algorithms for homogeneous UAVs and the optimal deployment with heterogeneous UAVs, where the service capacities on UAVs 1 and 2 are 10 and 30 users, respectively.

away from each other, since the communication range between any two UAVs is limited, e.g., a few hundred meters. Then, the total coverage area of the two UAVs may be overlapping, i.e., some users can be served by the two UAVs simultaneously. In addition, since different UAVs have different service capacities, the UAVs with large service capacities should be deployed over the places with high-density users, while the UAVs with low service capacities may be more likely to act as relays between the UAVs with large service capacities. However, existing studies in [10], [21], [30], [40], [42], and [46] for homogeneous UAVs deployment does not consider the different UAV service capacities, and a UAV with a low service capacity may be deployed to serve ground users, while a UAV with a large service capacity may serve as a relay in their delivered solutions.

The novelty of this paper lies in not only incorporating the heterogeneous service capacities of different UAVs into consideration, but also devising a novel approximation algorithm and an improved heuristic for the heterogeneous UAV deployment problem. Specifically, both the proposed algorithms deliver  $O(\sqrt{\frac{s}{K}})$ -approximate solutions, where K is the number of UAVs, s is a given positive integer with  $1 \le s \le K$ , e.g., s=3. Notice that the approximation ratio  $O(\sqrt{\frac{s}{K}})$  is better when the value of s is larger, this however incurs a longer running time.

#### C. Contributions

The main contributions of this paper are summarized as follows. We first formulate a novel maximum connected coverage problem for deploying a heterogeneous UAV network. We then devise an approximation algorithm for the problem and its approximation ratio is  $O(\sqrt{\frac{s}{K}})$ , followed with an improved heuristic algorithm, where s is a given positive integer. We finally evaluate the algorithm performance and our experimental results show that the number of users served by the proposed algorithms are up to 25% larger than those by existing algorithms.

The organization of this paper is as follows. Section II introduces the system model and defines the problem precisely. Section III and IV propose a novel approximation algorithm and an improved heuristic for the problem, respectively. Section V evaluates the performance of the proposed algorithms empirically. Section VI reviews related studies, and Section VII concludes this paper.

#### II. PRELIMINARIES

In this section, we first introduce the system and channel models. We then figure out the maximum number of users served by UAVs, assuming that UAVs have already been deployed. We finally define the problem precisely.

#### A. System Model

The deployed communication infrastructures in a disaster, e.g., an earthquake, a debris flow, or a flooding, might no longer function any more, due to the damages or power outage caused by the disaster. To evacuate people trapped in a disaster area, it is important to provide a temporarily emergent communication network for them. A promising solution is to deploy a UAV communication network.

Fig. 1 illustrates that a UAV network of four UAVs above a disaster area act as aerial base stations to provide communication service (e.g., LTE or WiFi) to people on the ground. There is at least one of the UAVs serving as the *gateway UAV*, which means that the UAV is connected to the Internet with the help of satellites or emergency communication vehicles. With the help of the UAV network, a person who is trapped in the disaster area can communicate with a nearby UAV, using his/her smartphone to send/receive critical information, such as voice and video, to/from the rescue team.

We treat the disaster zone as a 3-dimensional space with length  $\alpha$ , width  $\beta$ , and height  $\gamma$ , e.g.,  $\alpha=\beta=3$  km and  $\gamma=500$  m. Assume that there are n users  $u_1,u_2,\ldots,u_n$  in the disaster area, and let  $U=\{u_1,u_2,\ldots,u_n\}$ . Each user  $u_i\in U$  has a minimum data rate requirement  $r_i^{min}$ , e.g., 2 kbps, if the user is served by a UAV base station. Denote by  $(x_i,y_i,0)$  the coordinate of a user  $u_i$  with  $1\leq i\leq n$ . Assume that locations of the n users are given, where the location information can be derived by applying an existing target detection method [12], [14], [15] for the photos/vidoes taken by UAV on-board cameras.

We consider the employment of  $K \geq 2$  heterogeneous UAVs to provide communication service (e.g., LTE or WiFi) to affected people in the disaster area. Each UAV is equipped with a base station to serve as an aerial base station in the air [3]. Due to different maximum payloads and energy capacities on different UAVs, the base stations equipped on different UAVs have different capabilities. For example, since the maximum payload (i.e., 5.5 kg) [6] of a DJI Matrice 600 RTK UAV is larger than the payload (i.e., 2.7 kg) [7] of

a DJI Matrice 300 RTK UAV, the base station on the former may be more powerful, in terms of computing ability and/or battery capacity, thus is able to serve more users than the one on the latter UAV.

Denote by  $C_k$  the service capacity on the kth UAV with  $1 \le k \le K$ , which means that the UAV can provide communication service to at most  $C_k$  users simultaneously, e.g.,  $C_k = 100$  users. Notice that the service capacities of different UAVs usually are different. Following existing studies [4], [18], [21], [40], [43], [46], we assume that all UAVs hover at the same altitude  $H_{uav}$  to provide communication service to ground users, where  $H_{uav}$  is the optimal altitude for the maximum coverage from the air and the value of  $H_{uav}$  can be calculated by the algorithms in [2] and [42], e.g.,  $H_{uav} = 300$  meters. On the other hand, a ground user will receive a weaker signal from a UAV if the UAV hovers at a higher or lower altitude than the optimal altitude  $H_{uav}$ , which was both analytically and empirically validated in [2].

Since the base stations mounted on the K UAVs may have different capabilities, the transmission powers of the base stations on the UAVs are different, too. Denote by  $P_t^k$  the transmission power of the base station on the kth UAV with 1 < k < K.

For the sake of convenience, we divide the plane at altitude  $H_{uav}$  into equal size squares with a given side length  $\lambda$ , e.g.,  $\lambda=50$  meters. Assume that both the length  $\alpha$  and width  $\beta$  of the disaster area are divisible by the side length  $\lambda$ . Thus, the UAV hovering/service plane at altitude  $H_{uav}$  are partitioned into  $m=\frac{\alpha}{\lambda}\times\frac{\beta}{\lambda}$  grids. Let  $v_1,v_2,\ldots,v_m$  be the center locations of the m grids, respectively. Also, let  $V=\{v_1,v_2,\ldots,v_m\}$ . Assume that no more than one UAV can hover in a grid to avoid UAV collisions [46], i.e., two or more UAVs are not allowed to hover in the same grid.

#### B. Wireless Channel Models

We adopt similar UAV-to-user and UAV-to-UAV wireless channel models as those in [2], [40], and [46]. For the sake of convenience, we briefly introduce them as follows. On one hand, UAV-to-user wireless channels are so complicated as there may be obstacles, e.g., a building, between a UAV in the air and a user on the ground. Following existing studies, the UAV-to-user wireless channels are composed of Line-of-Sight (LoS) links and Non-Line-of-Sight (NLoS) links [2], [46]. Specifically, the pathloss  $PL_{i,j}$  between a ground user  $u_i$  and a UAV deployed at an aerial hovering location  $v_j$  is  $PL_{i,j} = P_{LoS} \cdot L_{LoS} + P_{NLoS} \cdot L_{NLoS}$ , where  $P_{LoS}$  is the LoS link probability and can be calculated by the method in [2],  $P_{NLoS} = 1 - P_{LoS}$ ,  $L_{LoS}$  and  $L_{NLoS}$  are the average pathlosses for LoS and NLoS links, respectively. In addition,  $L_{LoS} = 20 \log_{10} \frac{4\pi f_c d_{ij}}{c} + \eta_{LoS}, \ L_{NLoS} = 20 \log_{10} \frac{4\pi f_c d_{ij}}{c} + \eta_{NLoS}, \ \text{where} \ 20 \log_{10} \frac{4\pi f_c d_{ij}}{c} \ \text{is the free space passloss}, \ f_c \ \text{is the carrier frequency}, \ d_{ij} \ \text{is the Euclidean distance between}$ nodes  $u_i$  and  $v_i$ , c is the velocity of light,  $\eta_{LoS}$  and  $\eta_{NLoS}$ are the average shadow fadings in LoS and NLoS wireless connections, respectively.

The signal-to-noise ratio (SNR) received by user  $u_i$  from the UAV at location  $v_j$  then is  $SNR_{ij}=10^{\frac{P_t^j+g_t^j-PL_{i,j}-P_N}{10}}$ .

where  $P_t^j$  and  $g_t^j$  are the transmission power and antenna gain of the base station on the UAV, and  $P_N$  is the noise power. The average data rate  $r_{ij}$  of user  $u_i$  from the UAV at hovering location  $v_j$  then is  $r_{ij} = B_w \log_2(1 + SNR_{ij})$ , where  $B_w$  is the channel bandwidth allocated to user  $u_i$ , e.g.,  $B_w = 180 \ kHz$  when the OFDMA technique is used [28], [40].

Assume that the kth UAV at altitude  $H_{uav}$  can communicate with a ground user if their Euclidean distance is no greater than a given communication range  $R^k_{user}$ , where  $1 \leq k \leq K$ . This indicates that the communication coverage radii  $R^k_{user}$ s of different UAVs may be different, due to their different transmission powers and/or antenna gains.

On the other hand, UAV-to-UAV wireless channels can be modelled as the free space path loss [2], since there are usually no obstacles between any two UAVs in the air. We assume that any two UAVs can communicate with each other if their Euclidean distance is no more than a given communication range  $R_{uav}$ . The wireless connectivity technique among UAVs may be WiFi 802.11ad, FSO (Free Space Optics), or mmWave, where high bandwidth is available [34]. For example, WiFi 802.11ad offers a high bandwidth with 2 GHz and a reasonable communication range, e.g., 1 km. Notice that the value of  $R_{user}^k$  usually is smaller than  $R_{uav}$  [21], i.e.,  $R_{user}^k \leq R_{uav}$ .

#### C. Problem Definition

A UAV network is presented by an undirected graph  $G=(U\cup V,E)$ , where U is the set of n to-be-served users in the disaster area, V is the set of the m candidate UAV hovering locations at altitude  $H_{uav}$ . There is an edge  $(v_j,v_k)$  in the edge set E between two hovering locations  $v_j$  and  $v_k$  if their Euclidean distance is no more than the UAV communication range  $R_{uav}$ , and there is an edge  $(u_i,v_k)$  in E between a ground user  $u_i$  and a UAV hovering location  $v_k$  if their distance is no more than the communication coverage radius  $R_{user}^k$  of the UAV.

In this paper, we consider a maximum connected coverage problem in G, which is to choose K hovering locations  $v_1, v_2, \ldots, v_K$  among the m candidate hovering locations in V ( $K \leq m$ ), deploy K UAVs to the K chosen locations, respectively, and assign users to the K deployed UAVs, such that the number of users served by the UAVs is maximized, subject to following constraints that (i) each user  $u_i \in U$  is served by at most one UAV within its communication range  $R_{user}^k$  and the data rate is no less than its minimum data rate requirement  $r_i^{min}$ ; (ii) the number of users served by the kth UAV is no greater than its service capacity  $C_k$  with  $1 \leq k \leq K$ ; and (iii) the deployed UAV communication network is connected.

We note that users in a disaster zone may move around. In this scenario, an optimal deployment of UAVs may become sub-optimal sometimes later. We thus may need to re-deploy the UAVs by adopting the similar strategy in [40]. Specifically, after every fixed time period, e.g., 2 minutes, we invoke the proposed algorithms in Section III to find the updated optimal deployment locations for the K UAVs, where the most recent user location information can be detected and predicted from the photos taken by the on-board cameras of the UAVs [14],

[15]. If the number of served users under the previous UAV deployment locations is only slightly worse than the one under this new UAV deployment locations, e.g., no more than 5% smaller, the K UAVs do not fly to their new deployment locations, since users may experience interrupted service due to frequent changes of the network topology. Otherwise (the previous number of served users is at least 5% smaller than the new number), the K UAVs fly to their new deployment locations.

# D. The Optimal Assignment of Users With Given Deployed UAVs

Given K hovering locations  $v_1, v_2, \dots, v_K$ , assume that the kth UAV with service capacity  $C_k$  has already been deployed at location  $v_k$  in the air with  $1 \le k \le K$ . We here consider a maximum assignment problem, which is to assign users in U to the K deployed UAVs such that the number of users served by the UAVs is maximized, subject to the constraint that the number of users served by the UAV at location  $v_k$  is no greater than the service capacity  $C_k$  on the UAV. This problem serves as a subproblem of the maximum connected coverage problem in the previous Section II-C. There are two major differences between the two problems. The first one is that the K UAVs have been deployed in the former, while the to-be-deployed locations of the K UAVs are unknown in the latter, and the second one is that the deployed UAV communication network may be disconnected in the former, whereas the deployed UAV network must be connected in the latter.

We now propose an optimal algorithm for the maximum assignment problem, which will serve as a subroutine of the proposed algorithm for the maximum connected coverage problem. Given a set S of K hovering locations  $v_1, v_2, \ldots, v_K$ with |S| = K, assume that the kth UAV with service capacity  $C_k$  has already been deployed at location  $v_k$  with  $1 \le k \le K$ . A flow graph  $G' = (\{s\} \cup U \cup S \cup \{t\}, E')$  is first constructed, where nodes s and t are the source and sink nodes in the flow graph G', respectively. There is a directed edge  $\langle s, u_i \rangle$  in E'from s to each user  $u_i \in U$  with a capacity of one. There is a directed edge  $\langle u_i, v_k \rangle$  in E' from each user  $u_i \in U$ to each location  $v_k \in S$  if their Euclidean distance is no more than the communication range  $R_{user}^k$  of the kth UAV, and the data rate  $r_{ik}$  of user  $u_i$  is no less than its minimum data rate  $r_i^{min}$ . The capacity on edge  $\langle u_i, v_k \rangle$  is one. Finally, there is a directed edge  $\langle v_k, t \rangle$  in E' from each location  $v_k \in S$  to sink node t, and the edge capacity on it is the service capacity  $C_k$  of the UAV deployed at location  $v_k$ . Fig. 3 illustrates the construction of the flow graph G' with  $C_1 = 1$ and  $C_2 = 2$ .

Having constructed the flow graph G', we find an integral maximum flow in G' from s to t, by applying the algorithm in [1]. We obtain a feasible solution to the maximum assignment problem from the flow, where a user  $u_i$  is assigned to the UAV at location  $v_k$  if the flow of edge  $\langle u_i, v_k \rangle$  is one. For example, Fig. 3 shows that user  $u_1$  is assigned to the UAV at location  $v_1$ , and both users  $u_3$  and  $u_4$  are assigned to the UAV at location  $v_2$ . However, user  $u_2$  is not served by any UAV. Notice that the number of served users is equal to the value of the flow.

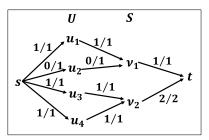


Fig. 3. An illustration of the construction of a flow graph G', where the numbers before and after a virgule '/' next to each edge mean the flow and capacity of the edge, respectively, the capacities of two UAVs are  $C_1=1$  and  $C_2=2$ , respectively, and the value of the maximum flow is 3.

Lemma 1: Given a set U of users, a set S of K hovering locations  $v_1, v_2, \ldots, v_K$ , the kth UAV with service capacity  $C_k$  has already been deployed at location  $v_k$  in S with  $1 \le k \le K$ . There is an algorithm for the maximum assignment problem in G, which delivers an optimal solution in time  $O(Kn^2)$ , where K = |S| and n = |U|.

*Proof:* The proof is contained in Section I of the supplementary file.  $\Box$ 

#### E. Notions of Submodular Functions and Matroids

Let N be a set of finite elements and f be a function with  $f: 2^N \mapsto \mathbb{R}^{\geq 0}$ . For any two subsets A and B of N with  $A \subseteq B$  and any element  $e \in N \setminus B$ , f is submodular if  $f(A \cup \{e\}) - f(A) \geq f(B \cup \{e\}) - f(B)$  [11], and f is monotone submodular if  $f(A) \leq f(B)$ .

A matroid  $\mathcal{M}$  is a pair  $(N,\mathcal{I})$ , where N is a set of elements and  $\mathcal{I}$  is a family of subsets of N with the following three properties [11]: (i)  $\emptyset \in \mathcal{I}$ ; (ii) the hereditary property: for any two sets A and B with  $A \subseteq B \subseteq N$ , if  $B \in \mathcal{I}$ , then  $A \in \mathcal{I}$ ; and (iii) the augmentation property: for any two sets A and B in  $\mathcal{I}$ , if A contains more elements than B (i.e., |A| > |B|), then there is an element  $e \in A \setminus B$  such that  $B \cup \{e\}$  is contained in  $\mathcal{I}$ , too.

# III. ALGORITHMS FOR THE MAXIMUM CONNECTED COVERAGE PROBLEM

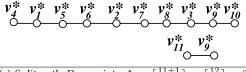
In this section, we study the maximum connected coverage problem in a large-scale disaster area. In this case, we choose the hovering locations of the K UAVs carefully, such that not only the number of users served by the deployed UAVs is maximized, but also the communication network formed by the UAVs is connected. We propose a novel  $O(\sqrt{\frac{s}{K}})$ -approximation algorithm for the problem with time complexity  $O(K^2n^2m^{s+1})$ , where s is a given positive integer, K is the number of UAVs, n is the number of users in the disaster area, and m is the number of candidate hovering locations. It can be seen that the approximation ratio  $O(\sqrt{\frac{s}{K}})$  is larger if the value of s is larger, which however incurs a longer running time.

# A. Basic Idea of the Approximation Algorithm

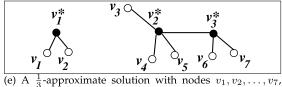
Assume that, in an optimal solution of the problem, the K UAVs are deployed at K hovering locations  $v_1^*, v_2^*, \ldots, v_K^*$ ,

(a) Duplicate the edge 
$$(v_9^*, v_{10}^*)$$
 in tree  $T^*$  but not in the longest path between nodes  $v_4^*$  and  $v_{11}^*$ 

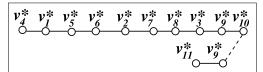
$$v_4^* v_1^* v_5^* v_6^* v_2^* v_7^* v_8^* v_3^* v_9^* v_{10}^*$$



(c) Split path  $P_{Euler}$  into  $\Delta = \lceil \frac{11+1}{L} \rceil = \lceil \frac{12}{10} \rceil = 2$  subpaths  $P_1$  and  $P_2$ , where L = 10.

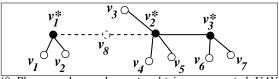


(e) A  $\frac{1}{3}$ -approximate solution with nodes  $v_1, v_2, \ldots, v$  and  $v_1^*, v_2^*, \ldots, v_3^*$  of the L nodes in  $P_j$ 



(b) A Eulerian path  $P_{Euler}$  that visits each edge in the graph of Fig. 4(b) and it has 11 edges.

(d) Subpath  $P_j$  consists of s nodes  $v_1^*, v_2^*, \dots, v_s^*$  and s+1 segments  $P_{j,1}, P_{j,2}, \dots, P_{j,s+1}$ , where s=3.



(f) Place a relay node  $v_8$  to obtain a connected UAV network

Fig. 4. An illustration of the basic idea of the proposed algorithm.

respectively. Let  $V^*=\{v_1^*,v_2^*,\ldots,v_K^*\}$ . Recall that in the maximum connected coverage problem, the induced subgraph  $G[V^*]$  by  $V^*$  is connected. Denote by  $T^*$  a spanning tree of  $G[V^*]$ , where  $T^*$  consists of the K nodes in  $V^*$  and K-1 edges. Let  $P^*$  be the longest path in tree  $T^*$ , e.g., the path between nodes  $v_4^*$  and  $v_{11}^*$  in Fig. 4(a). A Eulerian path  $P_{Euler}$  can be obtained by duplicating the edges in  $T^*$  but not in path  $P^*$ , see Fig. 4(a) and Fig. 4(b). The number of edges in the Eulerian path  $P_{Euler}$  is no more than  $2(K-1)-D^*$ , where  $D^*$  is the number of edges in path  $P^*$  with  $D^* \geq 1$ .

For any positive integer L with  $L \geq s$  (the optimal value of L will be calculated later in Section III-D), the Eulerian path  $P_{Euler}$  can be split into  $\Delta$  subpaths (or segments)  $P_1, P_2, \ldots, P_{\Delta}$ , such that the number of nodes in each subpath  $P_j$  is equal to L with  $1 \leq j \leq \Delta - 1$ , and the number of nodes in the last subpath  $P_{\Delta}$  is no greater than L, where

$$\Delta = \lceil \frac{2K - 2 - D^* + 1}{L} \rceil \le \lceil \frac{2K - 2}{L} \rceil, \quad \text{as } D^* \ge 1,$$
(1)

see Fig. 4(c). It can be seen that there is one subpath  $P_j$  among the  $\Delta$  subpaths such that the number of users served by the UAVs in  $P_j$  is no less than  $\frac{1}{\Delta}$  of the number of users served by the UAVs in tree  $T^*$ .

Consider any s nodes  $v_1^*, v_2^*, \ldots, v_s^*$  in subpath  $P_j$ , where the s nodes can be found by enumerating all possible candidates. It can be seen that  $P_j$  consists of the s nodes and s+1 segments  $P_{j,1}, P_{j,2}, \ldots, P_{j,s+1}$ , see Fig. 4(d). Denote by  $p_i$  the number of nodes in segment  $P_{j,i}$  with  $1 \le i \le s+1$ . For example, Fig. 4(d) shows that  $p_1 = 1$ ,  $p_2 = p_3 = p_4 = 2$  with s = 3. Let D be the sum of nodes in the s+1 segments, i.e.,  $D = \sum_{i=1}^{s+1} p_i = L - s$ , where there are L nodes in  $P_j$ .

The **basic idea** of the proposed algorithm is that, we observe that the L nodes in subpath  $P_j$  form a feasible solution to a submodular maximization problem, subject to the constraints

of  $\alpha(=2)$  matroids  $\mathcal{M}_1$  and  $\mathcal{M}_2$ , where  $\mathcal{M}_1$  and  $\mathcal{M}_2$  will be introduced later in Section III-B and Section III-C, respectively. We then can obtain a  $\frac{1}{\alpha+1}$   $(=\frac{1}{3})$  approximate solution V' with L nodes, by applying the algorithm in [11], where the s nodes  $v_1^*, v_2^*, \ldots, v_s^*$  must be contained in V'. Assume that  $V' = \{v_1, v_2, \ldots, v_D, v_1^*, v_2^*, \ldots, v_s^*\}$ , e.g., see Fig. 4(e) with D = L - s = 10 - 3 = 7. It can be seen that the number of users served by the UAVs deployed at locations in set V' is no less than  $\frac{1}{3}$  of the number of users served by the UAVs in  $P_j$ , thus no less than  $\frac{1}{3\Delta}$  of the number of users served by the UAVs in the optimal solution  $T^*$ , where  $\Delta \leq \lceil \frac{2K-2}{L} \rceil$  following Eq. (1).

Notice that the induced subgraph by G[V'] may be disconnected, e.g., see Fig. 4(e). We then place extra relaying nodes to obtain a connected UAV subnetwork, such that the nodes in V' are contained in the subnetwork. Fig. 4(f) shows that node  $v_8$  is added as a relay node between nodes  $v_1^*$  and  $v_2^*$ . Notice that the number of nodes in the connected subnetwork must be no greater than K.

In the following, we first define matroids  $\mathcal{M}_1$  and  $\mathcal{M}_2$  in Sections III-B and Section III-C, respectively, where the definition of  $\mathcal{M}_2$  depends on the value of L, and the s+1 numbers  $p_1, p_2, \ldots, p_{s+1}$ . We then calculate the optimal values of L and  $p_1, p_2, \ldots, p_{s+1}$  in Section III-D. We finally describe the approximation algorithm in Section III-E.

#### B. Definition of Matroid $\mathcal{M}_1$

Let X be the set of K UAVs, i.e.,  $X = \{1, 2, \ldots, K\}$ . Given the K UAVs in X and m hovering locations in V, we construct a set N of  $K \times m$  elements, where N is the Cartesian product of sets X and V, i.e.,  $N = \{ < k, v_j > \mid 1 \le k \le K, \ \forall v_j \in V \}$ . It can be seen that an element  $< k, v_j > \text{in } N$  indicates that the kth UAV with service capacity  $C_k$  will be deployed at location  $v_j$ .

Given any subset A of N, denote by f(A) the number of users served by the UAVs in A, which can be calculated by invoking the algorithm in Section II-D. For example, assume that  $A = \{ <1, v_1>, <2, v_2> \}$ , which means that UAVs 1 and 2 are deployed at locations  $v_1$  and  $v_2$ , respectively. Following the study in [24], function f(A) is submodular.

We define a set system  $\mathcal{M}_1=(N,\mathcal{I}_1)$  on set N, where  $\mathcal{I}_1$  is a family of subsets of N such that, for each set  $A\in\mathcal{I}_1$   $(A\subseteq N)$ , the number of pairs in A sharing the same UAV is no greater than one. In other words, each UAV cannot be placed at more than one location. For example,  $A_1=\{<1,v_1>\}$  is contained in  $\mathcal{I}_1$ , while  $A_2=\{<1,v_1>, <1,v_2>\}$  is not contained in  $\mathcal{I}_1$  as UAV 1 cannot be deployed at the two different locations  $v_1$  and  $v_2$ . The proof for the claim that  $\mathcal{M}_1$  is a matroid is similar to the one for Lemma 2 in [23] at page 10, omitted.

## C. Definition of Matroid $\mathcal{M}_2$

Consider any s nodes  $v_1^*, v_2^*, \ldots, v_s^*$  in subpath  $P_j$ , where there are L nodes in  $P_j$ , see Fig. 4(d). Subpath  $P_j$  consists of the s nodes and s+1 segments  $P_{j,1}, P_{j,2}, \ldots, P_{j,s+1}$ . Recall that there are  $p_i$  nodes in segment  $P_{j,i}$  with  $1 \le i \le s+1$ .

For any node  $v_l$  in  $P_j$ , denote by  $d_l$  the minimum number of hops in  $P_j$  between node  $v_l$  and nodes in the set  $\{v_1^*, v_2^*, \dots, v_s^*\}$ . For example, Fig. 4(d) shows that the shortest hop between node  $v_5^*$  and nodes in set  $\{v_1^*, v_2^*, v_3^*\}$  is only one. Let  $h_{max} = \max\{p_1, p_{s+1}, \max_{i=2}^s \lceil \frac{p_i}{2} \rceil \}\}$ , where  $h_{max}$  means the maximum shortest hops between nodes in  $P_j$  and nodes in the set  $\{v_1^*, v_2^*, \dots, v_s^*\}$ . For example, in Fig. 4(d), we know that  $p_1 = 1$ ,  $p_2 = p_3 = 2$ , and  $p_4 = 2$  with s = 3. Then,  $h_{max} = 2$ .

For each integer h with  $0 \le h \le h_{max}$ , denote by  $Q_h$  the number of nodes in  $P_j$  that are at least h hops away from the nodes in set  $\{v_1^*, v_2^*, \ldots, v_s^*\}$ . For example, Fig. 4(d) shows that  $Q_0 = 10$  since all the ten nodes in  $P_j$  are at least zero hop away from the nodes in  $\{v_1^*, v_2^*, v_3^*\}$ ,  $Q_1 = 7$  since the seven nodes  $v_4^*, v_5^*, \ldots, v_{10}^*$  are at least one hop away from the nodes in  $\{v_1^*, v_2^*, v_3^*\}$ , and  $Q_2 = 1$  since only node  $v_{10}^*$  is at least two hops away from the nodes in  $\{v_1^*, v_2^*, v_3^*\}$ .

We now formally define the value of  $Q_h$  with  $0 \le h \le h_{max}$ . Initially,  $Q_0 = L$ .

When  $1 \le h \le h_{max}$ , we then have

$$Q_h = \max\{p_1 - (h-1), 0\} + \sum_{i=2}^s \max\{p_i - 2(h-1), 0\} + \max\{p_{s+1} - (h-1), 0\}, \ 1 \le h \le h_{max}.$$
 (2)

Considering the L nodes in  $P_j$ , we define a family  $\mathcal{I}_2$  of subsets of V, such that for any subset V' in  $\mathcal{I}_2$ , the shortest hop between any node in V' and the nodes in  $\{v_1^*, v_2^*, \ldots, v_s^*\}$  is no more than  $h_{max}$ , and there are no more than  $Q_h$  nodes in V' that are at least h hops away from the nodes in set  $\{v_1^*, v_2^*, \ldots, v_s^*\}$ , where  $0 \leq h \leq h_{max}$ . We later show that  $\mathcal{M}_2 = (V, \mathcal{I}_2)$  is a matroid, see Lemma 1 in the supplementary file.

## D. Calculate the Optimal Values of L and $p_1, p_2, \ldots, p_{s+1}$

Consider any feasible solution V' in matroid  $\mathcal{M}_2$ , the induced subgraph by G[V'] may not be connected, see Fig. 4(e). We need to place extra relay nodes to ensure that the resulting graph become connected, so that nodes in V' are contained in the subnetwork. The number of deployed UAVs in the connected subnetwork is no greater than

$$g(L, p_1, p_2, \dots, p_{s+1})$$

$$= s + \sum_{i=2}^{s} p_i + \frac{p_1(p_1 + 1)}{2}$$

$$+ \sum_{i=2}^{s} \frac{p_i^2 + 2p_i + (p_i \bmod 2)}{4} + \frac{p_{s+1}(p_{s+1} + 1)}{2}, \quad (3)$$

and its proof is contained in Lemma 2 of the supplementary file

To serve more users, the value of L should be as large as possible. However, the number  $g(L, p_1, p_2, \ldots, p_{s+1})$  of deployed UAVs should be no greater than K UAVs.

In the following, we calculate the optimal values of L and  $p_1, p_2, \ldots, p_{s+1}$ . Denote by  $L_{max}$  the maximum value of L, and denote by  $p_1^*, p_2^*, \ldots, p_{s+1}^*$  the optimal numbers of  $p_1, p_2, \ldots, p_{s+1}$ , respectively, subject to the constraint that  $g(L_{max}, p_1^*, p_2^*, \ldots, p_{s+1}^*)$  is no greater than K.

We calculate the maximum value of  $L_{max}$  by binary search. It can be seen that  $s \leq L_{max} \leq K$ . Given a guess L of  $L_{max}$ , following Eq. (3), the number  $g(L, p_1, p_2, \ldots, p_{s+1})$  of deployed UAVs depends on the values of L, and  $p_1, p_2, \ldots, p_{s+1}$ . Denote by  $p_1^L, p_2^L, \ldots, p_{s+1}^L$  the optimal values of  $p_1, p_2, \ldots, p_{s+1}$ , respectively, for the fixed L, such that the number  $g(L, p_1, p_2, \ldots, p_{s+1})$  of deployed UAVs is minimized, where  $\sum_{i=1}^{s+1} p_i^L = L - s$ ,  $0 \leq p_i^L \leq L - s$  with  $1 \leq i \leq s+1$ . We calculate the values of  $p_1^L, p_2^L, \ldots, p_{s+1}^L$  as follows.

Given the value of L, we later show that, when the number  $g(L, p_1^L, p_2^L, \dots, p_{s+1}^L)$  of deployed UAVs is minimized, the difference of  $p_1^L$  and  $p_{s+1}^L$  is no greater than one, i.e.,  $|p_1^L - p_{s+1}^L| \leq 1$ , and the difference of  $p_i^L$  and  $p_{i'}^L$  is also no greater than one, i.e.,  $|p_i^L - p_{i'}^L| \leq 1$  with  $2 \leq i, i' \leq s$ , see Section II in the supplementary file. Without loss of generality, we assume that  $p_2^L \geq p_3^L \geq \cdots \geq p_s^L$ . Then,  $p_2^L - p_s^L \leq 1$ . Assume that there are j integers among the s-2 integers  $p_2^L, p_3^L, \dots, p_{s-1}^L$  so that they are larger than  $p_s^L$  by one. Let  $p=p_s^L$ . Then,  $p_2^L = p_3^L = \cdots = p_{j+1}^L = p+1$  while  $p_{j+2}^L = p_{j+3}^L = \cdots = p_s^L = p$ . Since the difference of  $p_1^L$  and  $p_{s+1}^L$  is no greater than one, let  $p_1^L = \lfloor \frac{L-s-\sum_{i=2}^s p_i^L}{2} \rfloor = \lfloor \frac{L-s-(s-1)p-j}{2} \rfloor$ , and  $p_{s+1}^L = \lceil \frac{L-s-(s-1)p-j}{2} \rceil$ .

It can be seen that the value of p is in the interval [0, L-s] and the value of j is in the interval [0, s-2]. Then, we can calculate the minimum number  $g(L, p_1^L, p_2^L, \ldots, p_{s+1}^L)$  of deployed UAVs and the values of  $p_1^L, p_2^L, \ldots, p_{s+1}^L$ , by considering all combinations of p and j.

The algorithm for calculating  $L_{max}$  and  $p_1^*, p_2^*, \ldots, p_{s+1}^*$  is presented in Algorithm 1. It can be seen that the time for finding the optimal value  $L_{max}$  and the optimal numbers  $p_1^*, p_2^*, \ldots, p_{s+1}^*$  is only  $O(s^2K \log K)$ .

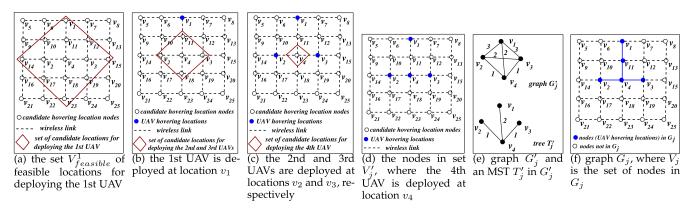


Fig. 5. An illustration of the execution of the approximation algorithm, where K = 5,  $L_{max} = 4$ , s = 1 and  $V_i^* = \{v_4\}$ .

**Algorithm 1** Calculate the Maximum Value of  $L_{max}$  and the Optimal Numbers  $p_1^*, p_2^*, \dots, p_{s+1}^*$ 

```
Input: The number K of UAVs and the value of s
Output: The values of L_{max} and p_1^*, p_2^*, \ldots, p_{s+1}^*
 1: Let L_{max} \leftarrow s; /* an initial value of L_{max} */
 2: Let L_{lb} \leftarrow s, L_{ub} \leftarrow K; /* L_{lb} and L_{ub} are lower and upper
     bounds on L_{max}, respectively */
 3: while L_{lb}+1 < L_{ub} do
4: Let L \leftarrow \lfloor \frac{L_{lb}+L_{ub}}{2} \rfloor; /* L is a guess of L_{max} */
        Let g(L, p_1^L, p_2^{\tilde{L}}, \dots, p_{s+1}^L) \leftarrow +\infty; for 0 \le p \le L - s, \ 0 \le j \le s - 2 do
 6:
            if (s-1)p+j \leq L-s then
 7:
                /* Ensure that the sum of p_2, p_3, \ldots, p_s, i.e., (s-1)p+j,
 8:
                is no greater than L-s; */
                Set p_2 = p_3 = \cdots = p_{j+1} = p+1, p_{j+2} = p_{j+3} =
 9:
                \cdots = p_s = p, \ p_1 = \lfloor \frac{L-s-(s-1)p-j}{2} \rfloor, \ \text{and} \ p_{s+1} = 0
10:
                Calculate the number g(L, p_1, p_2, \dots, p_{s+1}) of deployed
                UAVs by Eq. (3);
                if g(L, p_1, p_2, \dots, p_{s+1}) < g(L, p_1^L, p_2^L, \dots, p_{s+1}^L)
11:
                    Let p_i^L \leftarrow p_i with 1 \le i \le s+1;
12:
                end if
13:
14:
            end if
15:
         end for
        if g(L, p_1^L, p_2^L, \dots, p_{s+1}^L) \leq K then

Let L_{lb} \leftarrow L; /* updated lower bound on L_{max} */
16:
17:
            Let L_{max} \leftarrow L and p_i^* \leftarrow p_i^L with 1 \le i \le s+1;
18:
19:
20:
            Let L_{ub} \leftarrow L; /* updated upper bound on L_{max} */
21:
         end if
22: end while
23: return the values of L_{max} and p_1^*, p_2^*, \ldots, p_{s+1}^*.
```

#### E. Approximation Algorithm

Given a positive integer s, the proposed algorithm first calculates the optimal values of  $L_{max}$  and  $p_1^*, p_2^*, \ldots, p_{s+1}^*$ , by invoking Algorithm 1 in Section III-D.

For any subset  $V_j^*$  of V with s nodes, the proposed algorithm finds a connected subgraph  $G_j$  of G, where  $1 \leq j \leq {m \choose s}$ , m = |V| and  ${m \choose s}$  is the number of different ways of choosing s nodes from set V with m nodes. The solution to the problem then is the subgraph  $G_{j^*}$  among the  ${m \choose s}$  subgraphs such that the number of served users is maximized and the number of nodes in the subgraph is no greater than K, where

 $1 \leq j^* \leq {m \choose s}$ . In the following, we show how to find a connected subgraph  $G_j$ .

For any subset  $V_j^*$  of V with s nodes in V, let  $V_j^* = \{v_1^*, v_2^*, \dots, v_s^*\}$ . We define a submodular maximization problem, subject to the constraints of  $\alpha(=2)$  matroids  $\mathcal{M}_1$  and  $\mathcal{M}_2$ , where  $\mathcal{M}_1$  was defined in Section III-B, while  $\mathcal{M}_2$  was defined in Section III-C by replacing L with  $L_{max}$  and replacing  $p_i$  with  $p_i^*$  ( $1 \le i \le s+1$ ). For example, Fig. 5(a) shows the set V of candidate hovering locations. Assume that there are K=5 UAVs, and s=1. Then,  $L_{max}=4$ ,  $p_1^*=1$ ,  $p_2^*=2$  by invoking Algorithm 1. By the definition of matroid  $\mathcal{M}_2$  in Section III-C, we have  $h_{max}=2$ ,  $Q_0=4$ ,  $Q_1=3$ ,  $Q_2=1$ , following Eq. (2). In addition, assume that  $V_j^*=\{v_4\}$ . Then, a subset  $V_j'$  is contained in matroid  $\mathcal{M}_2$ , if every node in  $V_j'$  is no more than  $h_{max}=2$  hops away from  $v_4$ , and there are no more than  $Q_h$  nodes that are at least h hops away from  $v_4$ , where  $0 \le h \le 2$ .

We find an approximate solution  $V'_j$  with no more than  $L_{max}$  nodes to the submodular maximization problem under the constraints of matroids  $\mathcal{M}_1$  and  $\mathcal{M}_2$  as follows.

For the sake of convenience, we assume that  $C_1 \ge C_2 \ge \cdots \ge C_K$ , where  $C_k$  is the service capacity of the kth UAV with  $1 \le k \le K$ . The proposed algorithm consists of  $L_{max}$  iterations, and in the kth iteration we deploy the kth UAV with service capacity  $C_k$  at a hovering location, where  $L_{max} \le K$ .

Assume that before the kth iteration, UAVs  $1, 2, \ldots, k-1$  have already been deployed at hovering locations  $v_1, v_2, \ldots, v_{k-1}$ , respectively, i.e.,  $V'_j = \{v_1, v_2, \ldots, v_{k-1}\}$ . Also, denote by  $n_{k-1}$  the number of users served by the deployed k-1 UAVs, which can be calculated by invoking the algorithm in Section II-D that considers the connections between users and deployed UAVs.

In the kth iteration, we deploy the kth UAV at a hovering location  $v_k$  such that the increased number of users served by the UAV in maximized. Specifically, denote by  $V_{feasible}^k$  the set of nodes in  $V \setminus V_j'$  such that the set  $\{v_l\} \cup V_j'$  is contained in matroid  $\mathcal{M}_2$ , where  $v_l$  is in  $V \setminus V_j'$ , i.e.,  $V_{feasible}^k = \{v_l \mid (\{v_l\} \cup V_j') \in \mathcal{M}_2, \ v_l \in V \setminus V_j'\}$ . For example, Fig. 5(a) shows the set  $V_{feasible}^1$  of candidate hovering locations for deploying the first UAV, which is the set of nodes within two hops away from  $v_4$ . For each hovering location  $v_l \in V_{feasible}^k$  that has not been deployed a UAV in

the first k-1 iterations, we calculate the number  $n_{k,l}$  of users served the k UAVs  $1, 2, \dots, k$ , assuming that the kth UAV is deployed at location  $v_l$ . We then identify the location  $v_k$  in  $V_{feasible}^{k}$  such that the new increased number of users served is maximized, i.e.,  $v_k = \arg\max_{v_l \in V_{feasible}^k} \{n_{k,l} - n_{k-1}\}$ , where  $n_{k-1}$  is the number of users served by the deployed first k-1UAVs in the first k-1 iterations. For example, Fig. 5(b) shows that the first UAV is deployed at location  $v_1$ . The procedure continues until the hovering locations for UAVs  $1, 2, \dots, L_{max}$ are found, where  $L_{max} \leq K$ . The set of hovering locations for the  $L_{max}$  UAVs then is  $V'_j = \{v_1, v_2, \dots, v_{L_{max}}\}$ . For example, Fig. 5(b) shows the set of candidate locations for deploying the second and third UAVs, which is the set of nodes within one hop away from  $v_4$  (since there should be no more than  $Q_2 = 1$  node that is two hops away from  $v_4$  and the first UAV has already been deployed at node  $v_1$  that is exactly two hops away from  $v_4$ ). Then, assume that the second and third UAVs are deployed at locations  $v_2$  and  $v_3$ , respectively, see Fig. 5(c). We finally consider set of candidate hovering locations for deploying the fourth UAV. Since there are already three nodes in  $V'_i$  that are at least one hop away from  $v_4$  (i.e.,  $V'_i = \{v_1, v_2, v_3\}$ ), to ensure that the fourth UAV is deployed at a location v so that  $V_i' \cup \{v\}$  is still contained in matroid  $\mathcal{M}_2$ , the fourth UAV can be deployed at only location  $v_4$ , which is zero hop away from itself. The set of hovering locations for the  $L_{max} = 4$  UAVs then is  $V'_j = \{v_1, v_2, v_3, v_4\}$ , see Fig. 5(d).

It must be mentioned that the s nodes  $v_1^*, v_2^*, \dots, v_s^*$  in  $V_j^*$ must be contained in  $V_j'$ , as only nodes in  $V_j^*$  are zero hop away from  $V_i^*$  itself, and the number of nodes in  $V_i'$  that are zero hop away from  $V_i^*$  is  $Q_0 - Q_1 = s$ .

Recall that the kth UAV is deployed at hovering location  $v_k$  with  $1 \le k \le L_{max}$  and  $V'_j = \{v_1, v_2, \dots, v_{L_{max}}\}$ . Notice that the induced subgraph  $G[\check{V}'_i]$  by  $V'_i$  may not be connected, see Fig. 5(d). We construct a connected subgraph  $G_i$  of G such that the nodes in  $V'_i$  are contained in  $G_i$  as follows.

A weighted graph  $G'_j = (V'_j, E'_j)$  is first constructed from set  $V'_i$ , where there is an edge  $(v_k, v_l)$  in  $E'_i$  between any two nodes  $v_k$  and  $v_l$  in  $V'_i$ , and its edge weight  $w(v_k, v_l)$  is the minimum number of hops in G between them. A minimum spanning tree (MST)  $T'_j$  in  $G'_j$  is then found, see Fig. 5(e). Denote by  $q'_i$  the number of nodes in  $T'_i$ . For each edge  $(v_k, v_l)$ in tree  $T'_{j}$ , there is a corresponding shortest path  $P_{k,l}$  in graph G between nodes  $v_k$  and  $v_l$ .

A connected subgraph  $G_j$  of G can be obtained from  $T'_j$ , which is the union of the  $(q'_i - 1)$  shortest paths in G, i.e.,  $G_j = \{P_{k,l} \mid (v_k, v_l) \in T'_j\}$ , see Fig. 5(f). Denote by  $V_j$  the set of nodes in  $G_j$ . Also, let  $q_j = |V_j|$ . If the number  $q_j$  of nodes in  $G_i$  is greater than K, then  $G_i$  is not a feasible solution to the problem. Otherwise  $(q_i \leq K)$ , we deploy UAVs at the location node in  $G_j$  as follows.

Following the construction of  $G_j$ , it can be seen that the nodes in  $V'_i$  are contained in  $G_j$  (i.e.,  $V'_i$  is a subset of  $V_j$ ), where  $V'_j = \{v_1, v_2, \dots, v_{L_{max}}\}$  and the kth UAV with service capacity  $C_k$  has already been deployed at location node  $v_k$ with  $1 \leq k \leq L_{max}$ . We deploy UAVs  $L_{max} + 1, L_{max} +$  $2, \ldots, q_j$  at nodes in  $V_j \setminus V_j'$  in an arbitrary way, e.g., in a Algorithm 2 Approximation Algorithm for the Maximum Connected Coverage Problem in a Disaster Area (approAlg)

**Input:** A set U of users, a set V of candidate hovering locations, and K UAVs with service capacities  $C_1, C_2, \ldots, C_K$ , respectively Output: A solution to the maximum connected coverage problem

```
1: Calculates the optimal values of L_{max} and p_1^*, p_2^*, \dots, p_{s+1}^*,
```

- by invoking the algorithm in Section III-D; Let  $Q_0 \leftarrow L_{max}$  and define  $Q_h$  by Eq. (2),  $1 \le h \le h_{max}$ ;
- 3: Let  $n^* \leftarrow 0$ ; /\* the maximum number of served users \*/
- 4: **for** each subset  $V_i^*$  of V with s nodes **do**
- Sort the K UAVs by their service capacities in decreasing order, and assume that  $C_1 \geq C_2 \geq \cdots \geq C_K$ ;
- Let  $V'_j \leftarrow \emptyset$ ; /\* no UAVs are deployed initially \*/ 6:
- Let  $n_0 \leftarrow 0$ ; /\* no users are served initially \*/
- for  $1 \leq k \leq L_{max}$  do

  Find the set  $V_{feasible}^k$  of feasible location nodes for deploying the kth UAV, where  $V_{feasible}^k \leftarrow \{v_l \mid (\{v_l\} \cup V_j') \in V_j'\}$  $\mathcal{M}_2, \ v_l \in V \setminus V_j'\};$
- Deploy the kth UAV at a location node  $v_k$  in  $V_{feasible}^k$  such that the increased number of users served by the UAV in maximized, i.e.,  $v_k \leftarrow \arg\max_{v_l \in V_{feasible}^k} \{n_{k,l} - n_{k-1}\};$

```
Let V'_j \leftarrow V'_j \cup \{v_k\};
11:
```

end for 12:

13: Construct a graph  $G'_j = (V'_j, E'_j)$ , where there is an edge  $(v_k, v_l) \in E'_i$  between any two nodes  $v_k$  and  $v_l$  in  $V'_i$ , and its edge weight  $w(v_k, v_l)$  is the minimum number of hops between  $v_k$  and  $v_l$  in G;

Find a Minimum Spanning Tree (MST)  $T'_j$  in  $G'_j$ ;

Construct a connected subgraph  $G_j$  of G, where  $G_j$  =  $\{P_{k,l} \mid (v_k,v_l) \in T_j'\}$  and  $P_{k,l}$  is the shortest path in Gbetween nodes  $v_k$  and  $v_l$ . Let  $V_j$  be the set of nodes in  $G_j$ and  $q_j = |V_j|$ ;

if  $q_j \leq K$  then 16:

Deploy UAVs  $L_{max}+1, L_{max}+2, \ldots, q_j$  at location nodes in  $V_j \setminus V_j'$  in an arbitrary way;

Calculate the number  $n_i^*$  of users served by the deployed 18: UAVs in  $G_j$ ;

if  $n_i^* > n^*$  then 19:

/\* Find a better UAV deployment \*/ 20:

21: Let  $n^* \leftarrow n_i^*$  and  $j^* \leftarrow j$ ;

22:

23: end if

17:

24: end for

Assign users in U to the UAVs deployed in subgraph  $G_{j^*}$ , by invoking the algorithm in Section II-D;

26: **return** the deployment of UAVs in  $G_{j^*}$  and the assignment of users in U.

greedy way. For example, Fig. 5(f) shows that the fifth UAV is deployed at location  $v_{11}$ . The algorithm for the problem is presented in Algorithm 2.

# F. The Approximation Ratio Analysis

Theorem 1: Given a UAV network  $G = (U \cup V, E)$  and K UAVs with service capacities  $C_1, C_2, \ldots, C_K$ , respectively, there is an approximation algorithm, i.e., Algorithm 2, for the maximum connected coverage problem with time complexity of  $O(K^2n^2m^{s+1})$ , and the approximation ratio of the algorithm is  $\frac{1}{3\lceil \frac{2K-2}{L_1} \rceil} = O(\sqrt{\frac{s}{K}})$  and  $L_1 =$  $|\sqrt{4sK+4s^2-8.5s}|-2s+2$ , where n is the number of users in U (n = |U|) and m is the number of candidate hovering locations in V (m = |V|).

*Proof:* See the supplementary file.

#### IV. AN IMPROVED HEURISTIC

Following Eq. (1), the performance of Algorithm 2 is better when the value of L is larger. However, when the value of Lis too large, the number of nodes in the connected subnetwork  $G_i$  found at Step 15 in Algorithm 2 may be larger than the number K of available UAVs. On the other hand, recall that we estimated the upper bound  $g(L, p_1, p_2, \dots, p_{s+1})$  on the number of nodes in the connected subnetwork  $G_j$  with Eq. (3), and we can ensure that the number of nodes in  $G_i$  is no greater than K when its upper bound  $g(L, p_1, p_2, \dots, p_{s+1})$ is no more than K. Note that  $L_{max}$  is the largest integer such that  $g(L, p_1, p_2, \dots, p_{s+1}) \leq K$ . However, the estimated upper bound  $g(L, p_1, p_2, \dots, p_{s+1})$  may be conservative and the actual number of nodes in  $G_j$  may be less than the upper bound. Then, even if we adopt a value of L larger than the value  $L_{max}$  found by Algorithm 1, we may still find a connected subnetwork  $G_i$  with no more than K nodes. In this section, we propose a heuristic to improve the algorithm performance as follows.

For any fixed value of L between  $L_{max}$  found by Algorithm 1 and the number K of UAVs, we first find the optimal values  $p_1^L, p_2^L, \dots, p_{s+1}^L$  of  $p_1, p_2, \dots, p_{s+1}$  by invoking the pseudocodes from Step 5 to Step 15 in Algorithm 1, such that the value of  $g(L, p_1, p_2, \dots, p_{s+1})$  is minimized. Notice that the value of  $g(L, p_1^L, p_2^L, \dots, p_{s+1}^L)$  may be larger than K. We then find a connected subgraph  $G_L$  by invoking the pseudocodes from Step 3 to Step 24 in Algorithm 2. If the number of nodes in  $G_L$  is no greater than K, we may find a better solution than the one delivered by Algorithm 2. Denote by  $L_{improved}$  the maximum value of L such that the number of nodes in the found connected subgraph  $G_L$  is no greater than K, where  $L_{improved} \geq L_{max}$ . We can find the value of  $L_{improved}$  with a binary search. The improved heuristic algorithm for the problem is presented in Algorithm 3. It can be seen that the time complexity of Algorithm 3 is only a factor of  $O(\log K)$  larger than that of Algorithm 2.

## V. PERFORMANCE EVALUATION

In this section, we evaluated the performance of the proposed algorithms. In addition, we also investigated the impact of important parameters on the performance of the algorithms, including the number K of to-be-deployed UAVs, the value of parameter s, the number n of to-be-served users, the UAV service capacities, and the UAV communication range  $R_{uav}$ .

# A. Experimental Environment

Consider a disaster zone with a  $3\times 3~km^2$  square [46], in which 1,000 to 3,000 users are located. The user density follows a fat-tailed distribution, i.e., many users are located at a small portion of places while a few users are sparely located at many other places in the disaster zone [31]. The number K of UAVs varies from 2 to 20. The service capacity  $C_k$  of the kth UAV is randomly chosen from an interval of  $[C_{min}, C_{max}]$ , where  $C_{min}=50$  users,  $C_{max}=300$  users [40], and  $1\le k\le K$ . Each UAV hovers at an altitude  $H_{uav}=300~m$ 

Algorithm 3 Improved Heuristic Algorithm for the Maximum Connected Coverage Problem (approAlgPlus)

**Input:** A set U of users, a set V of candidate hovering locations, and K UAVs with service capacities  $C_1, C_2, \ldots, C_K$ , respectively **Output:** A solution to the maximum connected coverage problem

- 1: Calculates the values of  $L_{max}$  and  $p_1^*, p_2^*, \ldots, p_{s+1}^*$ , by invoking the algorithm in Section III-D;
- Let L<sub>improved</sub> ← L<sub>max</sub>; //L<sub>improved</sub> is the maximum value of L such that the number of nodes in the found connected subgraph is no greater than K.
- 3: Find a solution with  $L_{max}$  by invoking Algorithm 2, and let  $n_{improved}^*$  be the number of served users in the solution;
- 4: Let  $L_{lb} \leftarrow L_{max}$ ,  $L_{ub} \leftarrow K + 1$ ; //  $L_{lb}$  and  $L_{ub}$  are lower and upper bounds on  $L_{improved}$ , respectively.

```
5: while L_{lb} + 1 < L_{ub} do
6: // A binary search of L_{improved}
7: Let L \leftarrow \lfloor \frac{L_{lb} + L_{ub}}{2} \rfloor;
```

- 8: Find the optimal values  $p_1^L, p_2^L, \dots, p_{s+1}^L$  of  $p_1, p_2, \dots, p_{s+1}$  by invoking the pseudocodes from Step 5 to Step 15 in Algorithm 1;
- 9: Let  $Q_0 \leftarrow L$  and define  $Q_h$  by Eq. (2),  $1 \le h \le h_{max}$ ;
- 10: Find a connected subgraph  $G_L$  by invoking the pseudocodes from Step 3 to Step 24 in Algorithm 2, and let  $n_L$  be the number of served users in  $G_L$ ;

```
11:
       if the number of nodes in G_L is no greater than K then
          Let L_{lb} \leftarrow L; // update the lower bound
12:
          if n_L > n^*_{improved} then
13:
14:
              // Find a better solution
15:
              Let n_{improved}^* \leftarrow n_L;
              Let L_{improved} \leftarrow L;
16:
17:
          end if
18:
       else
19:
          Let L_{ub} \leftarrow L; // update the upper bound
20:
       end if
21: end while
22: Find the solution with L_{improved}.
```

to provide communication service to ground users [2]. The UAV communication range is  $R_{uav} = 600 \ m$ , while the user communication range is  $R_{user}^k = 500 \ m$  [46].

In addition to the proposed algorithms approAlg and approAlgPlus, we consider four benchmark algorithms. (i) Algorithm MCS [17] finds a  $\frac{1-1/e}{5(\sqrt{K}+1)}$ -approximate solution to cover as many users as possible by deploying K UAVs. (ii) Algorithm MotionCtrl [46] proposes a motion control solution to cover the maximum number of users by deploying a connected UAV network that consists of K UAVs. (iii) Algorithm greedyAssign [16] first assigns each candidate hovering location a profit in a greedy way, then deploys a network consisting of K UAVs, such that the sum of profits in the network is maximized. (iv) Algorithm maxThroughput [40] finds a  $\frac{1-1/e}{\sqrt{K}}$ -approximation solution to a problem of placing K homogenous UAVs, so that the network throughput is maximized. All experiment simulations were run on a server with an Intel(R) Core(TM) i5-9500 CPU (2.9 GHz) and 8 GB RAM.

# B. Algorithm Performance

We first study the performance of different algorithms by varying the number K from 2 to 20, when there are n=3,000 users and the parameter s is 1, 2, and 3, respectively. Fig. 6(a) shows that the number of served users by each

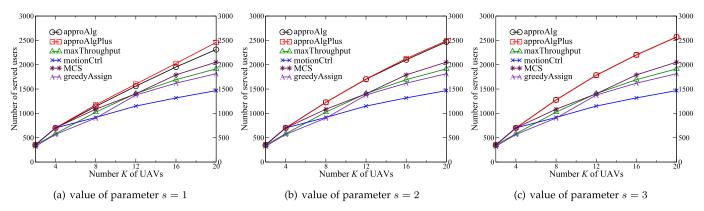
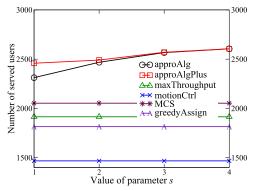


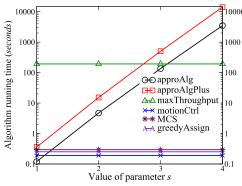
Fig. 6. The performance of different algorithms by increasing the number K of UAVs from 2 to 20, when there are n = 3,000 users, and s = 1,2, and 3, respectively.

algorithm increases with more UAVs deployed, when s = 1. It can be seen from Fig. 6(a) that the numbers of users served by both algorithms approAlg and approAlgPlus are up to 12% more than those by the other four algorithms when K = 20 UAVs. For examples, when K =20, the numbers of users served by algorithms approAlg, approAlgPlus, maxThroughput, MotionCtrl, MCS, and greedyAssign are 2,312, 2,458, 1,915, 1,467, 2,053, 1,815, respectively. In addition, Fig. 6(a) demonstrates that the number of users served by algorithm approAlgPlus is only slightly larger than the number by algorithm approAlq when  $K \leq 12$ , while the number by algorithm approAlgPlus is significantly larger than the number by algorithm approAlg when K > 12. For example, when K = 20, the number of users served by algorithm approAlgPlus is 6% larger than the number by algorithm approAlg. On the other hand, both Fig. 6(b) and Fig. 6(c) show that the number of users served by both algorithm approAlg or approAlgPlus is larger when s is larger.

We then deal with the tradeoff between the quality of the solution delivered by the proposed algorithms approAlg and approAlgPlus and their running times, by increasing the value of s from 1 to 4. Fig. 7(a) shows that the numbers of served users by both algorithms approAlg and approAlgPlus increase with the growth of parameter s, and the numbers are from 12% to 26% larger than those by the other four algorithms when s grows from 1 to 4. Furthermore, the gap between algorithms approAlg and approAlgPlus becomes smaller with the growth of s. Then, it can be seen from Fig. 6 and Fig. 7(a) that the number of users served by algorithm approAlgPlus is much larger than the number by algorithm approAlg when K is large (e.g., K = 20) and s is small (e.g., s = 1 or 2), whereas the number by algorithm approAlgPlus is only slightly larger than the number by algorithm approAlg when K is small or s is large. On the other hand, Fig. 7(b) plots that the running times of both algorithms approAlg and approAlgPlus also significantly increase with the growth of s, since their time complexity are  $O(K^2n^2m^{s+1})$ and  $O(K^2n^2m^{s+1}\log K)$ , respectively. Notice that in the application of deploying a UAV communication network to people trapped in a disaster area, we need the best tradeoff



(a) Number of served users by different algorithms



(b) Running time of different algorithms

Fig. 7. The performance of different algorithms by increasing the parameter s from 1 to 4, when there are n(=3,000) users and K(=20) UAVs.

between the quality of the delivered solution (i.e., the number of served users) and the algorithm running time. Fig. 6 and Fig. 7 indicate that we can find a good UAV deployment in a short time, e.g., within a few minutes, by either adopting algorithm approAlg with s=2 or 3, or using algorithm approAlgPlus with s=1 or 2. However, the running times of both algorithms approAlg and approAlgPlus with s=4 usually are unacceptable, which are as high as about 58 minutes and 3.9 hours, respectively.

We also investigate the algorithm performance by varying the number n of to-be-served users from 1,000 to 3,000, when there are K(=20) UAVs and s=3. Fig. 8 shows that

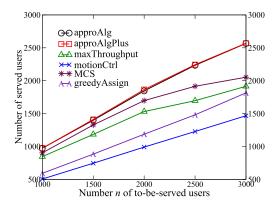


Fig. 8. The performance of different algorithms by varying the number n of to-be-served users from 1,000 to 3,000, when K=20 UAVs and s=3.

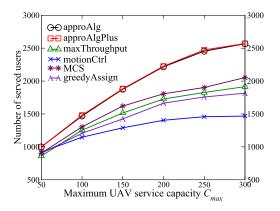


Fig. 9. The performance of different algorithms by varying the maximum UAV service capacity  $C_{max}$  from 50 to 300 users while fixing  $C_{min}=50$  users, when n=3,000 users, K=20 UAVs and s=3.

the numbers of users served by both algorithms approAlg and approAlgPlus are about from 7% to 25% more than those by algorithms maxThroughput, MotionCtrl, MCS, and greedyAssign respectively, with the growth of n from 1,000 to 3,000. Fig. 8 demonstrated that more users will be served by all comparison algorithms when there are more to-be-served users in the disaster area.

We further evaluate the algorithm performance by varying the maximum UAV service capacity  $C_{max}$  from 50 to 300 users while fixing  $C_{min}=50$ , where the service capacity of a UAV is randomly chosen from the interval  $[C_{min},C_{max}]$ . Fig. 9 demonstrates that the numbers of users served by both algorithms approAlg and approAlgPlus are from 10% to 25% larger than those by the other four algorithms, when  $C_{max}$  increases from 50 to 300 users.

We finally study the algorithm performance by varying the UAV communication range  $R_{uav}$  from 500 m to 1,000 m. Fig. 10 shows that more users will be served by each of the six algorithms and the number of users served by both algorithms approAlg and approAlgPlus are from 3% to 24% larger than those by the other four algorithms.

## VI. RELATED WORK

The deployment of UAV networks recently has gained lots of attentions in public communications. Most existing studies considered the deployment of *homogeneous UAVs*. For

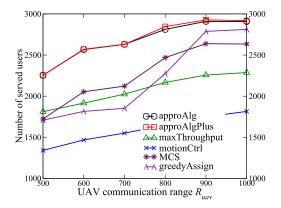


Fig. 10. The performance of different algorithms by varying the UAV communication range  $R_{uav}$  from 500 m to 1,000 m, when n=3,000 users, K=20 UAVs and s=3.

example, Zhao et al. [46] studied a problem of deploying a connected UAV network that consist of K UAVs to serve as many as users as possible, and they proposed a motion control algorithm for their problem. Liu et al. [21] investigated a similar problem in [46], and proposed an algorithm based on the deep reinforcement learning technique. Yang et al. [42] considered the problem of the flying trajectory planning of multiple UAVs, so as to provide emergent communication service to ground people. Shi et al. [30] considered the problem of finding UAV flying trajectories during a given period, in order to minimize the average pathloss between UAVs and users. Su et al. [33] studied the problem for jointly finding locations and power allocation of UAVs and the beamforming of STAR-RIS, to maximize the sum-rate of the UAV network. Fahim and Gadallah [10] studied the deployment of a single UAV to serve as many ground devices as possible. Xu et al. [40] recently studied a problem of deploying a connected UAV network that consists of K homogeneous UAVs in the air for monitoring a disaster area, such that the sum of data rates of all users is maximized, subject to the constraint that the number of users served by each UAV is no greater than its service capacity. They proposed a  $\frac{1-1/e}{\sqrt{K}}$ -approximation algorithm, where e is the base of the natural logarithm.

There are several studies on finding a connected subgraph with no more K nodes in a graph such that the value of a given submodular function over the K found nodes is maximized. For instance, Kuo et al. [17] studied a problem of placing a connected wireless network that consists of K wireless routers such that the number of users served is maximized, and proposed a  $\frac{1-1/e}{5(\sqrt{K}+1)}$ -approximation algorithm. Khuller et al. [16] investigated a problem of finding a connected subgraph with K nodes in a graph, such that the number of neighbouring nodes of the found K nodes is maximized. They proposed a  $\frac{1-1/e}{12}$ -approximation algorithm. However, the proposed algorithm is not applicable to the problem in this paper. Huang et al. [13] studied a problem of placing a connected sensor network that consists of K sensors, such that the number of targets monitored by the placed sensors is maximized, by designing a  $\frac{1-1/e}{8(\lceil 2\sqrt{2}\theta \rceil+1)^2}$ -approximation algorithm,

where  $0<\theta\leq 1$ . Yu et al. [44] recently proposed an improved algorithm and the approximation ratio is improved to  $\frac{1-1/e}{8(\lceil\frac{4}{\sqrt{3}}\theta\rceil+1)^2}$ . It can be seen that both the approximation ratios  $\frac{1-1/e}{8(\lceil2\sqrt{2}\theta\rceil+1)^2}$  [13] and  $\frac{1-1/e}{8(\lceil\frac{4}{\sqrt{3}}\theta\rceil+1)^2}$  [44] are between  $\frac{1-1/e}{128}$  and  $\frac{1-1/e}{32}$ , as  $0<\theta\leq 1$ . On the other hand, notice that there usually are tens or hundreds of UAVs to the deployed. In this case, the approximation ratio  $\frac{1-1/e}{\sqrt{K}}$  in [40] usually is larger than those in [13] and [44], i.e.,  $\frac{1-1/e}{\sqrt{K}}\geq \frac{1-1/e}{32}$  when  $K\leq 1,024$ . However, the solutions in these studies are inapplicable to the heterogeneous UAVs deployment.

In addition, we noticed that Wang et al. [36] first surveyed the most recent network and protocol architectures of multi-UAV-based heterogeneous flying ad hoc networks (FANET), then proposed novel distributed gateway-selection algorithms in UAV networks, and finally conceived a UAV cloud-control system to improve the limited computational capabilities of resource constrained mobile UAVs. It can be seen that the work in [36] did not address the problem of deploying UAV networks. In contrast, in this paper we studied a problem of deploying a UAV network in the air above a disaster area to serve as many trapped people as possible. We think that the studies in [36] and in this paper investigated different issues in UAV networks, thus are complementary.

#### VII. CONCLUSION

Different from existing studies that considered only the deployment of homogenous UAV networks, in this paper, we investigated the problem of deploying a heterogenous UAV network in a disaster so as to maximize the network throughput. We proposed a performance-guaranteed approximation algorithm and a heuristic algorithm for the deployment problem of the heterogenous UAV network. Extensive experimental results demonstrated that the UAV network by the proposed algorithms served 25% more users than those by existing algorithms.

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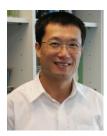
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