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1 Boolean expressions

Motivation

Boolean expressions and Boolean data type

2 Comparison operators

2.1 Comparison Operators (>, >=, ==, != etc.)

How to compare different values

Precedence and Associativity

Comparing **Different Data Types**

Using ! in python notebooks

Comparing **floating point numbers** and **absolute tolerance**

Review **isclose**

2.2 Boolean Operations (and, or, etc.)

Why use **boolean operators** (logical operators)

Truth Table

Chained logical operators

precedence and **associativity** for the logical operators

Short-circuit evaluation

Logical operators on non-boolean operands

3 Conditional Execution

Conditional Expression see 3.2

3.1 If-Then Construct

Sort 2 values

Indentation

pass - Leave the block empty

3.2 If-Then-Else Construct

if-statement with **else** clause

conditional expression

3.3 Nested Conditionals

Sort 3 values

nested if-statement with else clause

if-**elif**-else

eliminate duplicate checks

```
=====
```

More and Cheat notes

```
=====
```

1 Boolean expressions

Motivation

```
# Problem (division by zero)
def multiply_or_divide(a, b):
    print("a, b, a*b, a/b are: ", a, b, a * b, a / b, sep="\n")
multiply_or_divide(1, 2)
multiply_or_divide(1, 0)
```

Check and handle problem (I)

```
def multiply_or_divide(a, b):
    if b == 0: # == means comparison: same?
        print("a, b, a*b, a/b are: ", a, b, a * b, "undefined", sep="\n")
    else:
        print("a, b, a*b, a/b are: ", a, b, a * b, a / b, sep="\n")
```

```
multiply_or_divide(1, 0)
multiply_or_divide(1, 2)
```

Check and handle problem (I')

```
def multiply_or_divide(a, b):
    print("a/b: ", "undefined") if b==0 else print("a/b: ", a/b)
```

Check and handle problem (I'')

```
def multiply_or_divide(a, b):
    print("a/b:", a/b) if b!=0 else print("a/b:", "undefined")
    # b!=0 means "b is not equal to zero?"
```

Check and handle problem (I''')

```
def multiply_or_divide(a, b):
    print("a/b:", a/b) if b else print("a/b:", "undefined")
    # when we want true/false, but given a number b, then "b is non-zero" => true
```

Check and handle problem (II)

```
def multiply_or_divide(a, b):
    fix = a/b if b else "undefined"
    print("a, b, a*b, a/b are: ", a, b, a * b, fix, sep="\n")
```

```
multiply_or_divide(1, 0)
multiply_or_divide(1, 2)
```

Boolean expressions and Boolean data type

2.2 Boolean Operations (and, or, etc.)

Why use **boolean operators (logical operators)**

https://en.wikipedia.org/wiki/Functional_completeness

[Below is for interested students only](#)

<https://www.electronics-tutorials.ws/logic/universal-gates.html>

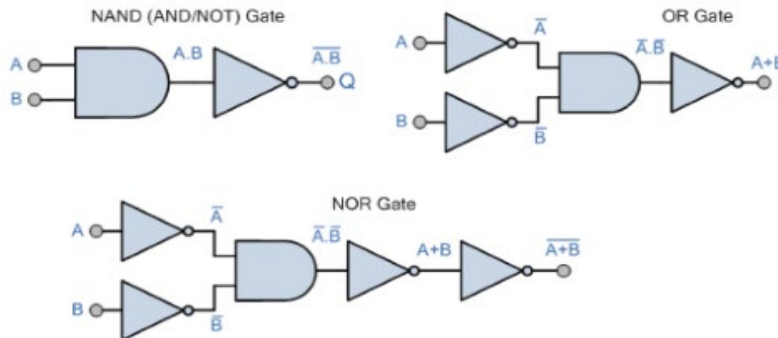
{AND} alone is not functionally complete

but

{AND, NOT} is functionally complete

we can use AND and NOT gates to make up other logic gates

AND/NOT Set Equivalents



Truth Table

Chained logical operators (See [Lecture03_Exercises](#))

precedence and **associativity** for the logical operators (See [Lecture03_Exercises](#))

Short-circuit evaluation (See [Lecture03_Exercises](#))

Logical operators on non-boolean operands (**Also See [Lecture03_Exercises](#)**)

Operators, Truth Table, Non-boolean Operands, Evaluation with Short-circuit evaluation

Operator	Description	Example
and	Return True when both statements are true	<code>x < 5 and x < 10</code>
or	Returns True when one of the statement is true	<code>x < 5 or x < 10</code>
not	Reverse the result, return True when the statement is False	<code>not (x < 5)</code>

x	y	x and y	x or y	not x
True	True	True	True	False
True	False	False	True	False
False	True	False	True	True
False	False	False	False	True

The above table is called a *truth table*. It enumerates all possible input and output combinations for each boolean operator.

Indeed, logical operators can even be applied to non-boolean operands.
From the [documentation](#):

In the context of Boolean operations, and also when expressions are used by control flow statements, the following values are interpreted as false:

`False` , `None` , numeric zero of all types, and empty strings and containers (including strings, tuples, lists, dictionaries, sets and frozensets).

All other values are interpreted as true.

Important

The expression `x or y` first evaluates `x` ;
if `x` is true, its value is returned;
otherwise, `y` is evaluated and the resulting value is returned.

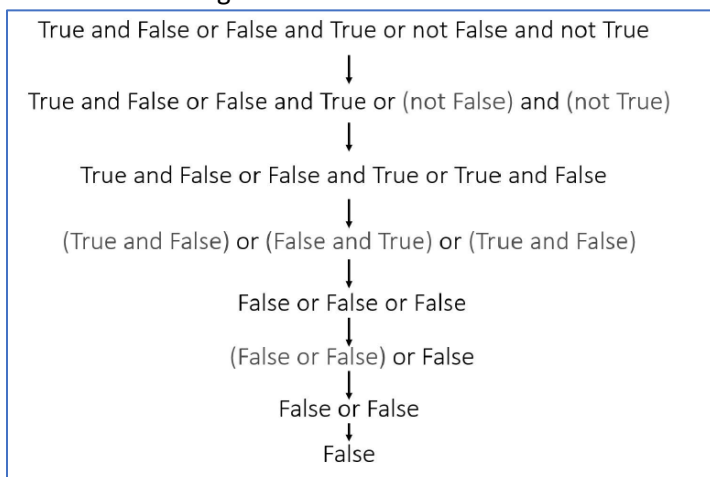
Important

The expression `x and y` first evaluates `x` ;
if `x` is false, its value is returned;
otherwise, `y` is evaluated and the resulting value is returned.

We know that number `0` means logical `False` and other numbers means logical `True`

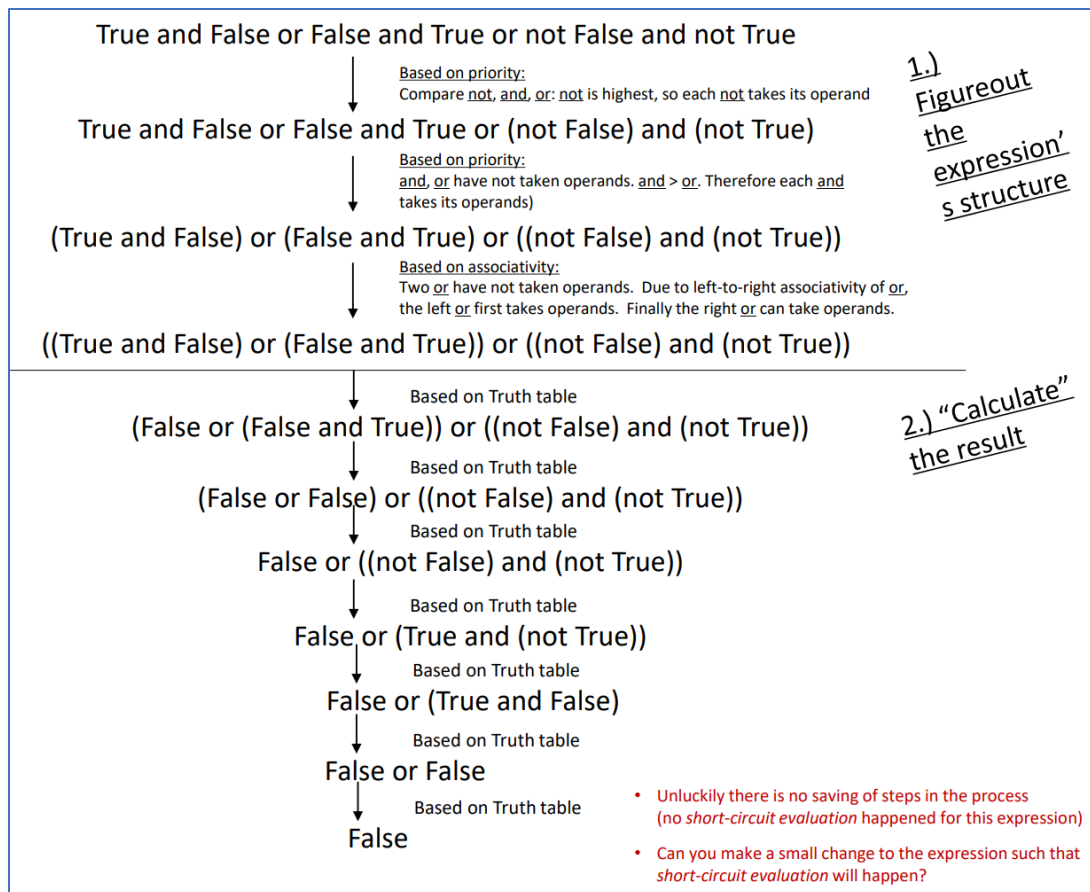
<code>x</code>	<code>y</code>	<code>x and y</code>	<code>x or y</code>	<code>not x</code>
<code>not 0</code>	<code>doesn't matter</code>	<code>y</code>	<code>x</code>	<code>False</code>
<code>0</code>	<code>doesn't matter</code>	<code>x</code>	<code>y</code>	<code>True</code>

The picture below is wrong:



The mistake: "(not False)" and "(not True)" should not be evaluated at the beginning.

The correct steps should be:



Testing

```
def returnFalse(label):
    print(label)
    return False
```

```
def returnTrue(label):
    print(label)
    return True
```

```
result1 = True and False or False and True or not False and not True
print(result1) # it shows False
```

```
result2 = returnTrue("a") and False or False and True or not returnFalse("b") and not returnTrue("c")
print(result2) # it shows a first: a b c False
```

To summarize:

Precedence and associativity of +, -, *, /, %, **, >, >=, <, <=, ==, !=, and, or, not

[Question]

What is meant by **precedence** of operators of arithmetic operations (Lec02), and comparisons and logical operations (Lec03)?

What does it apply to? How about **associativity** (Lec02)?

[Answer]

See the table below.

It lists some operators according to their *precedence* (~priority).

Upper ones have higher precedence than the lower ones.

(The contents are selected from <https://docs.python.org/3/reference/expressions.html#operator-precedence>)

Some common python operators in **descending order** of Precedence

Operator	Description
**	Exponentiation
-x	negative
*, /, //, %	Multiplication, division, floor division, remainder
+, -	Addition and subtraction
<, <=, >, >=, !=, ==	Comparisons and identity tests
not x	Boolean NOT
and	Boolean AND
or	Boolean OR
:=	Assignment expression

Note:

Operator precedence

Determines how operators are parsed concerning each other. Operators with higher precedence become the operands of operators with lower precedence.

(https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Operators/Operator_Precedence)

See this SIMPLE example on the right👉:

Associativity:

When two operators have the same precedence, **associativity** helps to determine the order of considerations.

(<https://www.programiz.com/python-programming/precedence-associativity>)

Consider $5*6 + 3**7$.
Will python do $5*6$ or $3**7$ first?

Answer: $5*6$ is done first (not 37)**

Student asks: "But ** has higher priority (precedence)!!"

Explanation:
The evaluate of an expression is based on its structure (a binary tree)

```
graph TD; A["+"] --- B["*"]; A --- C["**"]; B --- D["5"]; B --- E["6"]; C --- F["3"]; C --- G["7"];
```

precedence (priority) **doesn't** mean run **FIRST** or run **NEXT**
precedence (priority) is for **grouping** (how the expression structure is parsed)

In $5*6 + 3**7$,
** has higher precedence than +.
Therefore the result of $3**7$ becomes an operand of +.

That is:

- ** has highest priority. So, ** first takes 3 and 7 as its operands.
- * and + are left. Because * has higher priority, * can then take 5 and 6.
- Finally + takes its operands: $(5*6)$ and $(3**7)$

Well, for $(5*6) + (3**7)$, you and me will do $5*6$ first, agree? Same concept for Python ^_^

Conclusion: There are actually 2 steps:
Step 1: understand $5*6 + 3**7$ as $(5*6) + (3**7)$.
Step 2: based on $(5*6) + (3**7)$, calculate the left side $(5*6)$ to get 30, then calculate the right side $(3**7)$ to get 2187, then add 30 and 2187 to get 2217.

For binary arithmetic operators (+, -, *, /, %, ** ..) :

precedence: ** > * and / and % etc. > +, -
 associativity: ** is right-to-left; others are left-to-right
 e.g. $a**b**c$ means $a ** (b**c)$
 e.g. $a+b-c$ means $(a+b) - c$

For comparison operators (<, <=, >, >=, !=, ==) :

precedence: all are the same, and all are below + and -
 associativity: non-associative
 e.g. $a>b==c$ means $(a>b)$ and $(b==c)$

For logical operators (or we say "Boolean operators": and, or, not) :

precedence: not > and > or
 associativity: left-to-right
 e.g. a and b and c means $(a$ and $b)$ and c

For chained logical expression, truth table, short-circuit evaluation:

Evaluating chained Boolean expression

Stage 1.) Figure out the expression's structure

- Priority: **not** > **and** > **or**
- Associativity: **left associative** (A and B and C)

Stage 2.) "Calculate" the result

- Truth table:

x	y	x and y	x or y	not x
True	True	True	True	False
True	False	False	True	False
False	True	False	True	True
False	False	False	False	True
- Short-circuit evaluation:
 - True or B or C or D or E or... must be True
 - False and B and C and D and E and ... must be False

For involving non-boolean operands:

Important

The expression x or y first evaluates x :
 if x is true, its value is returned;
 otherwise, y is evaluated and the resulting value is returned.

Important

The expression x and y first evaluates x :
 if x is false, its value is returned;
 otherwise, y is evaluated and the resulting value is returned.

We know that number 0 means logical False, and other numbers means logical True:

x	y	x and y	x or y	not x
not 0	doesn't matter	y	x	False
0	doesn't matter	x	y	True

[To see explanations and examples, please refer to Lecture 2 and Lecture 3's notebooks (.ipynb)]

3 Conditional Execution

Conditional Expression see 3.2

3.1 If-Then Construct

Sort 2 values

Indentation

pass - Leave the block empty

3.2 If-Then-Else Construct

if-statement with **else** clause

conditional expression

3.3 Nested Conditionals

Sort 3 values

nested if-statement with else clause

if-**elif**-else

eliminate duplicate checks

```
=====
# if
x, y = 25, 25
if x <= y:
    print(x, y)
if y < x:
    print(y, x)

# "flow chart" (see lecture notebook: sort_two_values_fc1)

=====
# if
x, y = 25, 25
if x <= y: print(x, y)
if y < x: print(y, x)
=====
elderly = True
alone = True
disabled = True

# send a gift for elderly, or alone and disabled
gift = ____
if ____:
    gift = ____
if ____:
    if ____:
        gift = ____

print(gift) # expect True/False
=====
```

```

# if-else
x, y = 25, 25
if x <= y:
    print(x, y)
else:
    print(y, x)
=====

# if-else-pass
x, y = 25, 25

if x == y:
    pass # not yet decided what to output (leave this block empty)
else:
    if x < y:
        print(x, y)
    else:
        print(y, x)
=====

# if-else
x, y = 25, 25

if x == y:
    print("same:", x)
else:
    if x < y:
        print(x, y)
    else:
        print(y, x)
=====

# elif

x, y = 25, 25

if x == y:
    print("same:", x)
elif x < y:
    print(x, y)
else:
    print(y, x)
=====

# conditional expression
x, y = 40, 50

output1 = str(x) + " " + str(y)
output2 = str(y) + " " + str(x)

s = output1 if x <= y else output2
print(s)
=====

```

```
# conditional expression (ERROR 1!)
```

```
x, y = 40, 50
```

```
output1 = str(x) + " " + str(y)
```

```
output2 = str(y) + " " + str(x)
```

```
s = output1 if x <= y
```

```
print(s)
```

```
=====
```

```
# conditional expression (ERROR 2!)
```

```
x, y = 40, 50
```

```
output1 = str(x) + " " + str(y)
```

```
output2 = str(y) + " " + str(x)
```

```
s = output1 if x <= y else s = output2
```

```
print(s)
```

```
=====
```

```
elderly = True
```

```
alone = True
```

```
disabled = True
```

```
# send a gift for elderly, or alone and disabled
```

```
gift = _____ (No logical operators: and, or, not)
```

```
print(gift) # expect True/False
```

```
#Hint: gift = True if elderly else False if alone==False else True if disabled else False
```

```
=====
```

```
# sort 3 numbers
```

```
x, y, z = 10, 50, 1
```

```
if x <= y <= z: #this condition checks (x<=y) and (y<=z)
```

```
    print(x, y, z)
```

```
elif x <= z <= y:
```

```
    print(x, z, y)
```

```
elif y <= x <= z:
```

```
    print(y, x, z)
```

```
elif y <= z <= x:
```

```
    print(y, z, x)
```

```
elif z <= x <= y: #when we check this condition (z<=x) and (x<=y), actually the second part has already
```

```
    print(z, x, y) #been checked in the first condition
```

```
else:
```

```
    print(z, y, x)
```

```
=====
```

```
# sort 3 numbers (more efficient)
x,y,z=10,50,1
```

```
if x <= y:
    if y <= z:
        print(x, y, z)
    elif x <= z:
        print(x, z, y)
    else:
        print(z, x, y)
elif z <= y:
    print(z, y, x)
elif z <= x:
    print(y, z, x)
else:
    print(y, x, z)
```

=====

Self-study:

- go through the **lecture notebook** and **Readings**
- do EQuiz 3 (Available next Monday)